

**Homework 11**  
**for MATH 421**

From our text, please do problems 8.1 and 8.2. Then do the following problems.

- (A) Show that the free group on 3 generators is a subgroup of the free group on 2 generators.
- (B) Express the following groups  $\mathbb{Z}_{30}$ ,  $\mathbb{Z}^2 \times \mathbb{Z}_2$  and the quaternions as free groups modulo the appropriate relations.
- (C) Find a radical extension of  $\mathbb{Q}$  of the element  $(2 - \sqrt{3})^{\frac{1}{5}} - 3\sqrt[7]{4}(4 + \sqrt[13]{5})^{\frac{2}{9}}$ .