

## Homework 4 (due in class, Friday 3/11/16)

Let  $R$  be a relation and  $a$ ,  $b$ , and  $c$  belong to some set. Recall that

$aRa$  for all  $a$  means that  $R$  is reflexive

if  $aRb$ , then  $bRa$  for any  $a$  and  $b$  means that  $R$  is symmetric

if  $aRb$  and  $bRc$ , then  $aRc$  for any  $a, b, c$  means that  $R$  is transitive

1. Suppose  $aRb$  means that  $a$  and  $b$  are cousins. Is  $R$  reflexive?  
symmetric? transitive?
2. Suppose  $aRb$  means that  $a$  and  $b$  are sisters. Is  $R$  reflexive?  
symmetric? transitive?
3. Suppose  $aRb$  means that  $a$  is the sister of  $b$ . Is  $R$  reflexive?  
symmetric? transitive?
4. Suppose  $aRb$  means that  $a$  and  $b$  are musicians and have played in the same band. Is  $R$  reflexive? symmetric? transitive?
5. Think of an example of a relation  $R$  that hasn't been used in

class that is an equivalence relation – i.e., it is reflexive, symmetric, and transitive.