

## Chapter 12 – Introducing Probability

**12.1** In the long run, of a large number of five-card poker hands, the fraction in which you will be dealt a straight flush is about  $1/64,974$ . It *does not* mean that exactly 1 out of 64,974 such hands would yield a straight flush. The probability of an event is the long-run frequency of times the event occurs if the experiment is repeated endlessly ... not even almost 65,000 times.

**12.2 (a)** An impossible event has probability 0. **(b)** A certain event has probability 1. **(c)** A probability of 0.99 would correspond to an event that is very likely but will not occur once in a while in a long sequence of trials. **(d)** An event with probability 0.45 will occur slightly less often than it occurs (a bit less than 50% of the time).

**12.5 (a)**  $S = \{\text{lives on campus, lives off campus}\}$ . **(b)**  $S = \{\text{All numbers between _____ and _____ years}\}$ . (Choices of upper and lower limits will vary, most likely due to the characteristics of your institution.) **(c)**  $S = \{0000, 0001, 0002, \dots, 9999\}$ . **(d)**  $S = \{A, B, C, D, F\}$  (students might also include W, "+", and "-").

**12.9 (a)** Event  $B$  specifically rules out obese subjects, so there is no overlap with event  $A$ . **(b)**  $A$  or  $B$  is the event "The person chosen is overweight or obese."  $P(A \text{ or } B) = P(A) + P(B) = 0.36 + 0.33 = 0.69$ . **(c)**  $P(C) = 1 - P(A \text{ or } B) = 1 - 0.69 = 0.31$ .

**12.10 (a)**  $P(\text{either English or French}) = 0.083 + 0.789 = 0.872$ . **(b)**  $P(\text{other language}) = 1 - 0.872 = 0.128$ . **(c)**  $P(\text{not English}) = 1 - 0.083 = 0.917$ . (Or, add the other two probabilities.)

**12.11 (a)** Disjoint. **(b)** Not disjoint; \$300,000 is more than \$100,000 and more than \$250,000. **(c)** Disjoint;  $3 + x$  cannot equal 3.

**12.13 (a)**  $A = \{4, 5, 6, 7, 8, 9\}$ , so  $P(A) = 0.097 + 0.079 + 0.067 + 0.058 + 0.051 + 0.046 = 0.398$ . **(b)**  $B = \{2, 4, 6, 8\}$ , so  $P(B) = 0.176 + 0.097 + 0.067 + 0.051 = 0.391$ . **(c)**  $A$  or  $B = \{2, 4, 5, 6, 7, 8, 9\}$ , so  $P(A \text{ or } B) = 0.176 + 0.097 + 0.079 + 0.067 + 0.058 + 0.051 + 0.046 = 0.574$ . This is different from  $P(A) + P(B)$  because  $A$  and  $B$  are not disjoint.

**12.14 (a)** This is a legitimate probability model because the probabilities are all greater than 0 and sum to 1. **(b)** The event  $\{X < 4\}$  is the event that somebody eats dinner at home with his or her family 3 or fewer days per week.  $P(X < 4) = 0.05 + 0.00 + 0.07 + 0.08 = 0.20$ . **(c)** This is the event  $\{X \geq 1\}$ .  $P(X \geq 1) = 1 - P(X = 0) = 1 - 0.05 = 0.95$ .

**12.15 (a)**  $P(Y \leq 0.6) = 0.6$ . **(b)**  $P(Y < 0.6) = 0.6$ . **(c)**  $P(0.4 \leq Y \leq 0.8) = 0.4$ . **(d)**  $P(0.4 < Y \leq 0.8) = 0.4$ . The only difference between parts (c) and (d) is the inclusion of the point  $Y = 0.4$ . This has 0 probability for a continuous variable.

**12.17 (a)** This is  $P(X \geq 35)$ . **(b)**  $P(X \geq 35) = P\left(Z > \frac{35 - 25.3}{6.5}\right) = P(Z \geq 1.49) = 1 - 0.9319 = 0.0681$  (using Table A).

**12.22** (a) Probabilities express the *approximate* fraction of occurrences out of many trials.

**12.23** (b) The set  $\{0, 1, 2, 3, 4, 5\}$  lists all possible counts.

**12.24** (b) This is a finite model with a limited number of outcomes.

**12.25** (b) The other probabilities add to 0.97, so this must be 0.03.

**12.26** (b)  $P(\text{Republican or Democrat}) = P(\text{Republican}) + P(\text{Democrat}) = 0.25 + 0.30 = 0.55$ .

**12.27** (b)  $P(\text{not Republican}) = 1 - P(\text{Republican}) = 1 - 0.25 = 0.75$ .

**12.28** (b) There are ten equally likely possibilities, so  $P(\text{seven}) = 1/10$ .

**12.29** (c) "7 or greater" means 7, 8, or 9—three of the ten possibilities.

**12.30** (b) 22% ( $0.14 + 0.05 + 0.02 + 0.01 = 0.22$ , or 22%) have three or more cars.

**12.31** (c)  $Y > 1$  standardizes to  $Z > 2.56$ , for which Table A gives 0.0052.

**12.35** In computing the probabilities, we have dropped the trailing zeros from the land area figures. **(a)**  $P(\text{area is forested}) = 4176/9094 = 0.4592$  **(b)**  $P(\text{area is not forested}) = 1 - 0.4592 = 0.5408$

**12.51 (a)** This is a continuous random variable because the set of possible values is an interval. **(b)** The height should be  $1/2$  because the area under the curve must be 1. (For a rectangle, area =  $L \times W$ .) The density curve is illustrated. **(c)**  $P(Y \leq 1) = 1/2$

**12.52** For these probabilities, compute the areas of the appropriate rectangle under the density shown for Exercise 12.51. **(a)**  $P(0.5 < Y < 1.3) = (0.8)(0.5) = 0.4$  **(b)**  $P(Y \geq 0.8) = (1.2)(0.5) = 0.6$ .

