

Exam Review #2
Math 264
Exam date 10/18/2000

Topics Covered: Sections 12.1-12.5, 12.7-12.9

- **Functions of two and three variables**

- Domain and range.
- Graphs and level curves of functions of two variables.
- Level surfaces of functions of three variables.

- **Limits and continuity**

- Definition of limit and properties.
- Definition of continuity.
- The two-path test for non-existence of limits.

- **Partial derivatives**

- Definition and geometric interpretation.
- Higher order partial derivatives.
- The mixed derivative theorem.

- **Differentiability and linearization**

- Continuous partial derivatives imply differentiability.
- Linearization (tangent plane).
- Error in the standard linear approximation.

- **The chain rule**

- **Directional derivatives**

- Definition as a limit. Geometric interpretation.
- Relation between gradient and directional derivatives.
- Properties of directional derivatives: directions of maximum increase and decrease, direction of zero change (normal to gradient).
- Gradient is normal to level surfaces.

- **Optimization**

- Local maximum and minimum, saddle points.
- First derivative test. Critical points.
- Second derivative test.
- Absolute extrema on closed bounded regions.

- **Lagrange multipliers**

Study Problems - Chapter 12

- p. 994–998: 3, 5, 7, 9, 11, 15, 17, 19, 23, 25, 29, 31, 33, 35, 41, 43, 45, 49, 51, 53, 55, 57, 59, 61, 63, 65, 67, 71, 73, 79, 83, 87, 97 (practice problems).
- p. 998–999: 2, 7, 9, 13, 21, 23 (additional problems).