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1.  $X_1, X_2, \dots, X_n$  are iid with the following probability density function.

$$f(x_i|\theta) = \begin{cases} \frac{3}{\theta}e^{-3x_i/\theta}, & x_i > 0 \\ 0, & \textit{otherwise} \end{cases}$$

- a) Find the expected value of the  $X_i$ .

- b) Set  $\mu = E(X)$ . If  $n = 30$ ,  $\bar{X} = 3.1$  and  $S^2 = 9.4$ , find a 95% confidence interval for  $\mu$  (using t-procedures).

- c) Convert your interval for  $\mu$  to an interval for  $\theta$ . Hint: Write out your interval  $P(L \leq \mu \leq R)$  and then substitute  $\mu = E(X)$  which should be a function of  $\theta$ . Now solve the inequality for  $\theta$ .