viii

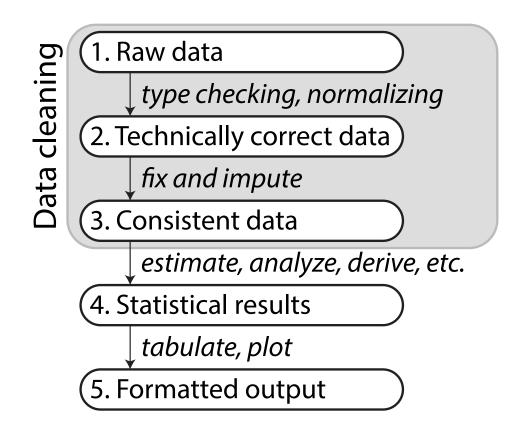
# Chapter 11 Data Cleaning

Data cleaning<sup>1</sup>, or data preparation, is an essential part of statistical analysis. In fact, in practice it is often more time-consuming than the statistical analysis itself. Data cleaning may profoundly influence the statistical statements based on the data. Typical actions like imputation or outlier handling obviously influence the results of a statistical analyses. For this reason, data cleaning should be considered a statistical operation, to be performed in a reproducible manner. The R statistical environment provides a good environment for reproducible data cleaning since all cleaning actions can be scripted and therefore reproduced.

# 11.1 The five steps of statistical analysis

Statistical analysis can be viewed as the result of a number of value-increasing data processing steps.

<sup>&</sup>lt;sup>1</sup>Content in this chapter is derived with permission from Statistics Netherlands at http://cran. r-project.org/doc/contrib/de\_Jonge+van\_der\_Loo-Introduction\_to\_data\_cleaning\_with\_R.pdf



Each box represents data in a certain state while each arrow represents the activities needed to get from one state to the other.

1. Raw Data The data "as is" may lack headers, contain wrong data types (e.g., numbers stored as strings), wrong category labels, unknown or unexpected character encoding and so on. Reading such files into an R data.frame directly is either difficult or impossible without some sort of preprocessing.

2. Technically correct data The data can be read into an R data.frame, with correct names, types and labels, without further trouble. However, that does not mean that the values are error-free or complete.

For example, an age variable may be reported negative, an under-aged person may be registered to possess a driver's license, or data may simply be missing. Such inconsistencies obviously depend on the subject matter that the data pertains to, and they should be ironed out before valid statistical inference from such data can be produced.

**3. Consistent data** The data is ready for statistical inference. It is the data that most statistical theories use as a starting point. Ideally, such theories can still be applied without taking previous data cleaning steps into

account. In practice however, data cleaning methods like imputation of missing values will influence statistical results and so must be accounted for in the following analyses or interpretation thereof.

4. Statistical results The results of the analysis have been produced and can be stored for reuse.

**5.** Formatted output The results in tables and figures ready to include in statistical reports or publications.

**Best practice** Store the input data for each stage (raw, technically correct, consistent, results, and formatted) separately for reuse. Each step between the stages may be performed by a separate R script for reproducibility.

# 11.2 R background review

## 11.2.1 Variable types

The most basic variable in R is a vector. An R vector is a sequence of values of the same type. All basic operations in R act on vectors (think of the element-wise arithmetic, for example). The basic types in R are as follows.

**numeric** Numeric data (approximations of the real numbers)

integer Integer data (whole numbers)

**factor** Categorical data (simple classifications, like gender)

ordered Ordinal data (ordered classifications, like educational level)

character Character data (strings)

raw Binary data (rarely used)

All basic operations in R work element-wise on vectors where the shortest argument is recycled if necessary. Why does the following code work the way it does?

```
# vectors have variables of _one_ type
c(1, 2, "three")
## [1] "1" "2" "three"
# shorter arguments are recycled
(1:3) * 2
```

## [1] 2 4 6
(1:4) \* c(1, 2)
## [1] 1 4 3 8
# warning! (why?)
(1:4) \* (1:3)
## Warning in (1:4) \* (1:3): longer object length is not a multiple of shorter object length
## [1] 1 4 9 4

## 11.2.2 Special values and value-checking functions

Below are the definitions and some illustrations of the special values NA, NULL,  $\pm \texttt{Inf},$  and <code>NaN</code>.

• NA Stands for "not available". NA is a placeholder for a missing value. All basic operations in R handle NA without crashing and mostly return NA as an answer whenever one of the input arguments is NA. If you understand NA, you should be able to predict the result of the following R statements.

```
NA + 1
sum(c(NA, 1, 2))
median(c(NA, 1, 2, 3), na.rm = TRUE)
length(c(NA, 2, 3, 4))
3 == NA
NA == NA
TRUE | NA
# use is.na() to detect NAs
is.na(c(1, NA, 3))
```

• NULL Think of NULL as the empty set from mathematics; it has no class (its class is NULL) and has length 0 so it does not take up any space in a vector.

```
length(c(1, 2, NULL, 4))
sum(c(1, 2, NULL, 4))
x <- NULL
length(x)
c(x, 2)
# use is.null() to detect NULL variables
is.null(x)</pre>
```

• Inf Stands for "infinity" and only applies to vectors of class numeric (not integer). Technically, Inf is a valid numeric that results from calculations like division of a number by zero. Since Inf is a numeric, operations be-

UNM, Stat 427/527 ADA1

tween Inf and a finite numeric are well-defined and comparison operators work as expected.

```
pi/0
2 * Inf
Inf - 1e+10
Inf + Inf
3 < -Inf
Inf == Inf
# use is.infinite() to detect Inf variables
is.infinite(-Inf)</pre>
```

• NaN Stands for "not a number". This is generally the result of a calculation of which the result is unknown, but it is surely not a number. In particular operations like 0/0, Inf - Inf and Inf/Inf result in NaN. Technically, NaN is of class numeric, which may seem odd since it is used to indicate that something is not numeric. Computations involving numbers and NaN always result in NaN.

```
NaN + 1
exp(NaN)
# use is.nan() to detect NULL variables
is.nan(0/0)
```

Note that is.finite() checks a numeric vector for the occurrence of any non-numerical or special values.

```
is.finite(c(1, NA, 2, Inf, 3, -Inf, 4, NULL, 5, NaN, 6))
## [1] TRUE FALSE TRUE FALSE TRUE FALSE TRUE FALSE TRUE
```

# 11.3 From raw to technically correct data

## 11.3.1 Technically correct data

Limiting ourselves to "rectangular" data sets read from a text-based format, **technically correct** data in R

- 1. is stored in a data.frame with suitable columns names, and
- 2. each column of the data.frame is of the R type that adequately represents the value domain.

The second demand implies that numeric data should be stored as numeric or integer, textual data should be stored as character and categorical data should be stored as a factor or ordered vector, with the appropriate levels.

**Best practice** Whenever you need to read data from a foreign file format, like a spreadsheet or proprietary statistical software that uses undisclosed file formats, make that software responsible for exporting the data to an open format that can be read by R.

## 11.3.2 Reading text data into an R data.frame

In the following, we assume that the text-files we are reading contain data of at most one unit per line. The number of attributes, their format and separation symbols in lines containing data may differ over the lines. This includes files in fixed-width or csv-like format, but excludes XML-like storage formats.

#### Reading text

read.table() and similar functions below will read a text file and return a
data.frame.

**Best practice.** A freshly read data.frame should always be inspected with functions like head(), str(), and summary().

The read.table() function is the most flexible function to read tabular data that is stored in a textual format. The other read-functions below all eventually use read.table() with some fixed parameters and possibly after some preprocessing. Specifically

- read.csv() for comma separated values with period as decimal separator.
- read.csv2() for semicolon separated values with comma as decimal separator.
- read.delim() tab-delimited files with period as decimal separator.
- read.delim2() tab-delimited files with comma as decimal separator.
- read.fwf() data with a predetermined number of bytes per column.

Additional optional arguments include:

Argument	Description	
header	Does the first line contain column names?	
col.names	character vector with column names.	
na.string	Which strings should be considered NA?	
colClasses	character vector with the types of columns. Will	
	coerce the columns to the specified types.	
stringsAsFactors	If TRUE, converts all character vectors into factor vec-	
	tors.	
sep	Field separator.	

Except for read.table() and read.fwf(), each of the above functions assumes by default that the first line in the text file contains column headers. The following demonstrates this on the following text file.

21,6.0 42,5.9 18,5.7\* 21,NA

Read the file with defaults, then specifying necessary options.

```
fn.data <- "http://statacumen.com/teach/ADA2/ADA2_notes_Ch18_unnamed.txt"</pre>
# first line is erroneously interpreted as column names
person <- read.csv(fn.data)</pre>
person
     X21 X6.0
##
## 1 42 5.9
## 2 18 5.7*
## 3 21 <NA>
# instead, use header = FALSE and specify the column names
person <- read.csv(file = fn.data</pre>
                  , header = FALSE
                  , col.names = c("age", "height")
                  )
person
     age height
##
## 1 21
            6.0
            5.9
## 2 42
## 3 18
           5.7*
## 4 21
           <NA>
```

If colClasses is not specified by the user, read.table() will try to determine the column types. Although this may seem convenient, it is noticeably slower for larger files (say, larger than a few MiB) and it may yield unexpected results. For example, in the above script, one of the rows contains a malformed numerical variable (5.7\*), causing R to interpret the whole column as a text variable. Moreover, by default text variables are converted to factor, so we are now stuck with a height variable expressed as levels in a categorical variable:

```
str(person)
```

```
## 'data.frame': 4 obs. of 2 variables:
## $ age : int 21 42 18 21
## $ height: Factor w/ 3 levels "5.7*","5.9","6.0": 3 2 1 NA
```

As an alternative, columns can be read in as character by setting stringsAsFactors Next, one of the as.-functions can be applied to convert to the desired type, as shown below.

```
person <- read.csv(file = fn.data</pre>
                 , header = FALSE
                  , col.names = c("age", "height")
                  , stringsAsFactors = FALSE)
person
##
     age height
## 1 21
         6.0
## 2 42
           5.9
## 3 18 5.7*
## 4 21 <NA>
person$height <- as.numeric(person$height)</pre>
## Warning: NAs introduced by coercion
person
##
     age height
## 1 21
            6.0
## 2 42
            5.9
## 3 18
             NA
## 4 21
             NA
```

Now, everything is read in and the height column is translated to numeric, with the exception of the row containing 5.7\*. Moreover, since we now get a warning instead of an error, a script containing this statement will continue to run, albeit with less data to analyse than it was supposed to. It is of course up to the programmer to check for these extra NA's and handle them appropriately.

## 11.4 Type conversion

Converting a variable from one type to another is called coercion. The reader is probably familiar with R's basic coercion functions, but as a reference they are listed here.

UNM, Stat 427/527 ADA1

as.numeric
as.integer
as.character
as.logical
as.factor
as.ordered
Each of these functions takes an R object and tries to convert it to the class
specified behind the "as.". By default, values that cannot be converted to the
specified type will be converted to a NA value while a warning is issued.

```
as.numeric(c("7", "7*", "7.0", "7,0"))
## Warning: NAs introduced by coercion
## [1] 7 NA 7 NA
```

In the remainder of this section we introduce R's typing and storage system and explain the difference between R types and classes. After that we discuss date conversion.

#### 11.4.1 Introduction to R's typing system

Everything in R is an object. An object is a container of data endowed with a label describing the data. Objects can be created, destroyed, or overwritten on-the-fly by the user. The function class returns the class label of an R object.

```
class(c("abc", "def"))
## [1] "character"
class(1:10)
## [1] "integer"
class(c(pi, exp(1)))
## [1] "numeric"
class(factor(c("abc", "def")))
## [1] "factor"
# all columns in a data.frame
sapply(dalton.df, class)
##
                     birth
          name
                                  death
                 "numeric"
## "character"
                            "numeric"
```

For the user of R these class labels are usually enough to handle R objects in R scripts. Under the hood, the basic R objects are stored as C structures as C is the language in which R itself has been written. The type of C structure that is used to store a basic type can be found with the typeof function. Compare the results below with those in the previous code snippet.

```
typeof(c("abc", "def"))
## [1] "character"
typeof(1:10)
## [1] "integer"
typeof(c(pi, exp(1)))
## [1] "double"
typeof(factor(c("abc", "def")))
## [1] "integer"
```

Note that the type of an R object of class numeric is double. The term double refers to double precision, which is a standard way for lower-level computer languages such as C to store approximations of real numbers. Also, the type of an object of class factor is integer. The reason is that R saves memory (and computational time!) by storing factor values as integers, while a translation table between factor and integers are kept in memory. Normally, a user should not have to worry about these subtleties, but there are exceptions (the homework includes an example of the subtleties).

In short, one may regard the class of an object as the object's type from the user's point of view while the type of an object is the way R looks at the object. It is important to realize that R's coercion functions are fundamentally functions that change the underlying type of an object and that class changes are a consequence of the type changes.

## 11.4.2 Recoding factors

In R, the value of categorical variables is stored in factor variables. A factor is an integer vector endowed with a table specifying what integer value corresponds to what level. The values in this translation table can be requested with the levels function.

```
f <- factor(c("a", "b", "a", "a", "c"))
f
### [1] a b a a c
### Levels: a b c
levels(f)
### [1] "a" "b" "c"
as.numeric(f)</pre>
```

UNM, Stat 427/527 ADA1

## [1] 1 2 1 1 3

You may need to create a translation table by hand. For example, suppose we read in a vector where 1 stands for male, 2 stands for female and 0 stands for unknown. Conversion to a factor variable can be done as in the example below.

```
# example:
gender <- c(2, 1, 1, 2, 0, 1, 1)
gender
## [1] 2 1 1 2 0 1 1
# recoding table, stored in a simple vector
recode <- c(male = 1, female = 2)</pre>
recode
     male female
##
        1
               2
##
gender <- factor(gender, levels = recode, labels = names(recode))
gender
## [1] female male
                             female <NA>
                     male
                                           male
                                                   male
## Levels: male female
```

Note that we do not explicitly need to set NA as a label. Every integer value that is encountered in the first argument, but not in the levels argument will be regarded missing.

Levels in a factor variable have no natural ordering. However in multivariate (regression) analyses it can be beneficial to fix one of the levels as the reference level. R's standard multivariate routines (lm, glm) use the first level as reference level. The relevel function allows you to determine which level comes first.

```
gender <- relevel(gender, ref = "female")
gender
## [1] female male male female <NA> male male
## Levels: female male
```

Levels can also be reordered, depending on the mean value of another variable, for example:

```
age <- c(27, 52, 65, 34, 89, 45, 68)
gender <- reorder(gender, age)
gender
## [1] female male male female <NA> male male
## attr(,"scores")
## female male
## 30.5 57.5
## Levels: female male
```

Here, the means are added as a named vector attribute to gender. It can be removed by setting that attribute to NULL.

```
attr(gender, "scores") <- NULL
gender
## [1] female male male female <NA> male male
## Levels: female male
```

## 11.4.3 Converting dates

The base R installation has three types of objects to store a time instance: Date, POSIX1t, and POSIXct. The Date object can only be used to store dates, the other two store date and/or time. Here, we focus on converting text to POSIXct objects since this is the most portable way to store such information.

Under the hood, a **POSIXct** object stores the number of seconds that have passed since January 1, 1970 00:00. Such a storage format facilitates the calculation of durations by subtraction of two **POSIXct** objects.

When a POSIXct object is printed, R shows it in a human-readable calender format. For example, the command Sys.time() returns the system time provided by the operating system in POSIXct format.

```
current_time <- Sys.time()
class(current_time)
## [1] "POSIXct" "POSIXt"
current_time
## [1] "2015-08-29 16:20:25 MDT"</pre>
```

Here, Sys.time() uses the time zone that is stored in the locale settings of the machine running R.

Converting from a calender time to POSIXct and back is not entirely trivial, since there are many idiosyncrasies to handle in calender systems. These include leap days, leap seconds, daylight saving times, time zones and so on. Converting from text to POSIXct is further complicated by the many textual conventions of time/date denotation. For example, both 28 September 1976 and 1976/09/28 indicate the same day of the same year. Moreover, the name of the month (or weekday) is language-dependent, where the language is again defined in the operating system's locale settings.

The lubridate package contains a number of functions facilitating the conversion of text to POSIXct dates. As an example, consider the following code.

```
library(lubridate)
dates <- c("15/02/2013"
                          , "15 Feb 13"
                         , "It happened on 15 02 '13")
dmy(dates)
## [1] "2013-02-15 UTC" "2013-02-15 UTC" "2013-02-15 UTC"</pre>
```

Here, the function dmy assumes that dates are denoted in the order daymonth-year and tries to extract valid dates. Note that the code above will only work properly in locale settings where the name of the second month is abbreviated to Feb. This holds for English or Dutch locales, but fails for example in a French locale (Fevrier).

There are similar functions for all permutations of d, m, and y. Explicitly, all of the following functions exist.

dmy()
dym()
mdy()
myd()
ydm()
ymd()

So once it is known in what order days, months and years are denoted, extraction is very easy.

**Note** It is not uncommon to indicate years with two numbers, leaving out the indication of century. Recently in R, 00-69 was interpreted as 2000-2069 and 70-99 as 1970-1999; this behaviour is according to the 2008 POSIX standard, but one should expect that this interpretation changes over time. Currently all are now 2000-2099.

```
dmy("01 01 68")
## [1] "2068-01-01 UTC"
dmy("01 01 69")
## [1] "2069-01-01 UTC"
dmy("01 01 90")
## [1] "2090-01-01 UTC"
dmy("01 01 00")
## [1] "2000-01-01 UTC"
```

It should be noted that lubridate (as well as R's base functionality) is only

capable of converting certain standard notations. For example, the following notation does not convert.

```
dmy("15 Febr. 2013")
## Warning: All formats failed to parse. No formats found.
## [1] NA
```

The standard notations that can be recognized by R, either using lubridate or R's built-in functionality are shown below. The complete list can be found by typing ?strptime in the R console. These are the day, month, and year formats recognized by R.

Code	Description	Example
%a	Abbreviated weekday name in the current locale.	Mon
%A	Full weekday name in the current locale.	Monday
%b	Abbreviated month name in the current locale.	Sep
<b>%</b> В	Full month name in the current locale.	September
%m	Month number $(01-12)$	09
%d	Day of the month as decimal number $(01-31)$ .	28
%y	Year without century (00-99)	13
%Y	Year including century.	2013

Here, the names of (abbreviated) week or month names that are sought for in the text depend on the locale settings of the machine that is running R.

If you know the textual format that is used to describe a date in the input, you may want to use R's core functionality to convert from text to POSIXct. This can be done with the as.POSIXct function. It takes as arguments a character vector with time/date strings and a string describing the format.

```
dates <- c("15-9-2009", "16-07-2008", "17 12-2007", "29-02-2011")
as.POSIXct(dates, format = "%d-%m-%Y")
## [1] "2009-09-15 MDT" "2008-07-16 MDT" NA
## [4] NA</pre>
```

In the format string, date and time fields are indicated by a letter preceded by a percent sign (%). Basically, such a %-code tells R to look for a range of substrings. For example, the %d indicator makes R look for numbers 1-31 where precursor zeros are allowed, so 01, 02, ..., 31 are recognized as well. Strings that are not in the exact format specified by the format argument (like the third string in the above example) will not be converted by as.POSIXct. Impossible dates, such as the leap day in the fourth date above are also not converted.

Finally, to convert dates from POSIXct back to character, one may use the format function that comes with base R. It accepts a POSIXct date/time object and an output format string.

```
mybirth <- dmy("28 Sep 1976")
format(mybirth, format = "I was born on %B %d, %Y")
## [1] "I was born on September 28, 1976"</pre>
```

# 11.5 From technically correct data to consistent data

Consistent data are technically correct data that are fit for statistical analysis. They are data in which missing values, special values, (obvious) errors and outliers are either removed, corrected, or imputed. The data are consistent with constraints based on real-world knowledge about the subject that the data describe.

Consistency can be understood to include **in-record consistency**, meaning that no contradictory information is stored in a single record, and **crossrecord consistency**, meaning that statistical summaries of different variables do not conflict with each other. Finally, one can include cross-dataset consistency, meaning that the dataset that is currently analyzed is consistent with other datasets pertaining to the same subject matter. In this tutorial *we mainly focus on methods dealing with in-record consistency*, with the exception of outlier handling which can be considered a cross-record consistency issue.

The process towards consistent data always involves the following three steps.

• **Detection** of an inconsistency. That is, one establishes which constraints are violated. For example, an age variable is constrained to nonnegative values.

- Selection of the field or fields causing the inconsistency. This is trivial in the case of a univariate demand as in the previous step, but may be more cumbersome when cross-variable relations are expected to hold. For example the marital status of a child must be unmarried. In the case of a violation it is not immediately clear whether age, marital status, or both are wrong.
- Correction of the fields that are deemed erroneous by the selection method. This may be done through deterministic (model-based) or stochastic methods.

For many data correction methods these steps are not necessarily neatly separated.

First, we introduce a number of techniques dedicated to the detection of errors and the selection of erroneous fields. If the field selection procedure is performed separately from the error detection procedure, it is generally referred to as **error localization**. Next, we describe techniques that implement correction methods based on "direct rules" or "deductive correction". In these techniques, erroneous values are replaced by better ones by directly deriving them from other values in the same record. Finally, we give an overview of some commonly used imputation techniques that are available in R.

## 11.5.1 Detection and localization of errors

This section details a number of techniques to detect univariate and multivariate constraint violations.

#### Missing values

A missing value, represented by NA in R, is a placeholder for a datum of which the type is known but its value isn't. Therefore, it is impossible to perform statistical analysis on data where one or more values in the data are missing. One may choose to either omit elements from a dataset that contain missing values or to impute a value, but missingness is something to be dealt with prior to any analysis.

In practice, analysts, but also commonly used numerical software may confuse a missing value with a default value or category. For instance, in Excel 2010, the result of adding the contents of a field containing the number 1 with an empty field results in 1. This behaviour is most definitely unwanted since Excel silently imputes "0" where it should have said something along the lines of "unable to compute". It should be up to the analyst to decide how empty values are handled, since a default imputation may yield unexpected or erroneous results for reasons that are hard to trace.

Another commonly encountered mistake is to confuse an NA in categorical data with the category *unknown*. If *unknown* is indeed a category, it should be added as a factor level so it can be appropriately analyzed. Consider as an example a categorical variable representing place of birth. Here, the category *unknown* means that we have no knowledge about where a person is born. In contrast, NA indicates that we have no information to determine whether the birth place is known or not.

The behaviour of R's core functionality is completely consistent with the idea that the analyst must decide what to do with missing data. A common choice, namely "leave out records with missing data" is supported by many base functions through the na.rm option.

```
age <- c(23, 16, NA)
mean(age)
## [1] NA
mean(age, na.rm = TRUE)
## [1] 19.5</pre>
```

Functions such as sum(), prod(), quantile(), sd(), and so on all have this option. Functions implementing bivariate statistics such as cor() and cov() offer options to include complete or pairwise complete values.

Besides the is.na() function, that was already mentioned previously, R comes with a few other functions facilitating NA handling. The complete.cases() function detects rows in a data.frame that do not contain any missing value.

Recall the person data set example from earlier.

```
print(person)
## age height
## 1 21 6.0
## 2 42 5.9
## 3 18 NA
## 4 21 NA
complete.cases(person)
## [1] TRUE TRUE FALSE FALSE
```

The resulting logical can be used to remove incomplete records from the data.frame. Alternatively the na.omit() function, does the same.

```
persons_complete <- na.omit(person)
persons_complete
## age height
## 1 21 6.0
## 2 42 5.9
na.action(persons_complete)
## 3 4
## 3 4
## attr(,"class")
## [1] "omit"</pre>
```

The result of the na.omit() function is a data.frame where incomplete rows have been deleted. The row.names of the removed records are stored in an attribute called na.action.

**Note.** It may happen that a missing value in a data set means 0 or Not applicable. If that is the case, it should be explicitly imputed with that value, because it is not unknown, but was coded as empty.

#### Special values

As explained previously, numeric variables are endowed with several formalized special values including  $\pm Inf$ , NA, and NaN. Calculations involving special values often result in special values, and since a statistical statement about a real-world phenomenon should never include a special value, it is desirable to handle special values prior to analysis. For numeric variables, special values indicate values

that are not an element of the mathematical set of real numbers. The function is.finite() determines which values are "regular" values.

is.finite(c(1, Inf, NaN, NA))
## [1] TRUE FALSE FALSE FALSE

This function accepts vectorial input. With little effort we can write a function that may be used to check every numerical column in a data.frame.

```
f.is.special <- function(x) {</pre>
  if (is.numeric(x)) {
    return(!is.finite(x))
  } else {
    return(is.na(x))
}
person
##
     age height
## 1 21
            6.0
            5.9
## 2
    42
## 3 18
             NA
     21
## 4
             NA
sapply(person, f.is.special)
##
          age height
## [1,] FALSE FALSE
## [2,] FALSE FALSE
## [3,] FALSE
                TRUE
## [4,] FALSE
                TRUE
```

Here, the f.is.special() function is applied to each column of person using sapply(). f.is.special() checks its input vector for numerical special values if the type is numeric, otherwise it only checks for NA.

## 11.5.2 Edit rules for detecting obvious inconsistencies

An obvious inconsistency occurs when a record contains a value or combination of values that cannot correspond to a real-world situation. For example, a person's age cannot be negative, a man cannot be pregnant and an under-aged person cannot possess a drivers license.

Such knowledge can be expressed as *rules* or constraints. In data editing

literature these rules are referred to as *edit rules* or *edits*, in short. Checking for obvious inconsistencies can be done straightforwardly in R using logical indices and recycling. For example, to check which elements of  $\mathbf{x}$  obey the rule ' $\mathbf{x}$  must be non negative' one simply uses the following.

```
x_nonnegative <- (x >= 0)
```

However, as the number of variables increases, the number of rules may increase rapidly and it may be beneficial to manage the rules separate from the data. Moreover, since multivariate rules may be interconnected by common variables, deciding which variable or variables in a record cause an inconsistency may not be straightforward.

The editrules package allows one to define rules on categorical, numerical or mixed-type data sets which each record must obey. Furthermore, editrules can check which rules are obeyed or not and allows one to find the minimal set of variables to adapt so that all rules can be obeyed. The package also implements a number of basic rule operations allowing users to test rule sets for contradictions and certain redundancies.

As an example, we will work with a small file containing the following data.

```
age,agegroup,height,status,yearsmarried
21,adult,6.0,single,-1
2,child,3,married, 0
18,adult,5.7,married, 20
221,elderly, 5,widowed, 2
34,child, -7,married, 3
```

We read this data into a variable called people and define some restrictions on age using editset().

```
fn.data <- "http://statacumen.com/teach/ADA2/ADA2_notes_Ch18_people.txt"</pre>
people <- read.csv(fn.data)</pre>
people
     age agegroup height status yearsmarried
##
## 1 21
            adult
                     6.0 single
                                            -1
                                            0
## 2 2
            child
                     3.0 married
                     5.7 married
                                            20
## 3 18 adult
## 4 221 elderly
                     5.0 widowed
                                             2
## 5
     34
         child
                    -7.0 married
                                             3
library(editrules)
E <- editset(c("age >=0", "age <= 150"))</pre>
```

UNM, Stat 427/527 ADA1

```
E
##
## Edit set:
## num1 : 0 <= age
## num2 : age <= 150
```

The editset() function parses the textual rules and stores them in an editset object. Each rule is assigned a name according to it's type (numeric, categorical, or mixed) and a number. The data can be checked against these rules with the violatedEdits() function. Record 4 contains an error according to one of the rules: an age of 221 is not allowed.

violatedEdits(E, people)
## edit
## record num1 num2
## 1 FALSE FALSE
## 2 FALSE FALSE
## 3 FALSE FALSE
## 4 FALSE TRUE
## 5 FALSE FALSE

violatedEdits() returns a logical array indicating for each row of the data, which rules are violated. The number and type of rules applying to a data set usually quickly grow with the number of variables. With editrules, users may read rules, specified in a limited R-syntax, directly from a text file using the editfile() function. As an example consider the contents of the following text file (note, you can't include braces in your if() statement).

```
# numerical rules
age >= 0
height > 0
age <= 150
age > yearsmarried
# categorical rules
status %in% c("married", "single", "widowed")
agegroup %in% c("child", "adult", "elderly")
if ( status == "married" ) agegroup %in% c("adult","elderly")
# mixed rules
if ( status %in% c("married", "widowed")) age - yearsmarried >= 17
if ( age < 18 )
                           agegroup == "child"
if ( age >= 18 && age <65 ) agegroup == "adult"
if ( age >= 65 )
                             agegroup == "elderly"
```

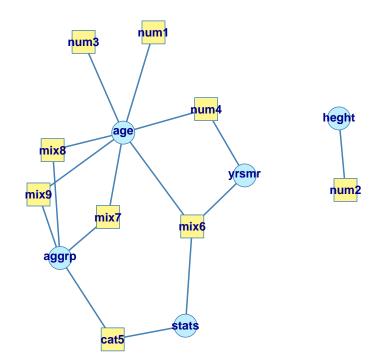
There are rules pertaining to purely numerical, purely categorical and rules pertaining to both data types. Moreover, there are univariate as well as multivariate rules. Comments are written behind the usual # character. The rule set can be read as follows.

```
fn.data <- "http://statacumen.com/teach/ADA2/ADA2_notes_Ch18_edits.txt"</pre>
E <- editfile(fn.data)</pre>
F.
##
## Data model:
## dat6 : agegroup %in% c('adult', 'child', 'elderly')
## dat7 : status %in% c('married', 'single', 'widowed')
##
## Edit set:
## num1 : 0 <= age
## num2 : 0 < height
## num3 : age <= 150
## num4 : yearsmarried < age</pre>
## cat5 : if( agegroup == 'child' ) status != 'married'
## mix6 : if( age < yearsmarried + 17 ) !( status %in% c('married', 'widowed') )</pre>
## mix7 : if( age < 18 ) !( agegroup %in% c('adult', 'elderly') )</pre>
## mix8 : if( 18 <= age & age < 65 ) !( agegroup %in% c('child', 'elderly') )</pre>
## mix9 : if( 65 <= age ) !( agegroup %in% c('adult', 'child') )</pre>
```

Since rules may pertain to multiple variables, and variables may occur in several rules (e.g., the age variable in the current example), there is a dependency between rules and variables. It can be informative to show these dependencies in a graph using the plot function. Below the graph plot shows the interconnection of restrictions. Blue circles represent variables and yellow boxes represent restrictions. The lines indicate which restrictions pertain to what variables.

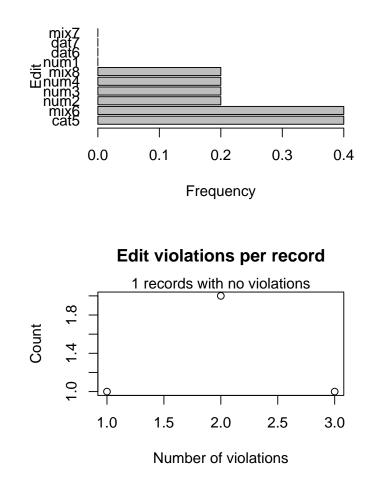
```
op <- par(no.readonly = TRUE)  # save plot settings
par(mfrow=c(1,1), mar = c(0,0,0,0))
plot(E)
par(op)  # restore plot settings</pre>
```

UNM, Stat 427/527 ADA1



As the number of rules grows, looking at the full array produced by violatedEdits( becomes cumbersome. For this reason, editrules offers methods to summarize or visualize the result.

```
ve <- violatedEdits(E, people)</pre>
summary(ve)
## Edit violations, 5 observations, 0 completely missing (0%):
##
##
    editname freq rel
                 2 40%
##
        cat5
                 2 40%
##
        mix6
                 1 20%
##
        num2
                 1 20%
##
        num3
                 1 20%
##
        num4
##
        mix8
                 1 20%
##
##
   Edit violations per record:
##
    errors freq rel
##
##
          0
               1 20%
               1 20%
##
          1
##
          2
               2 40%
          3
               1 20%
##
plot(ve)
```



Edit violation frequency of top 10 edits

Here, the edit labeled cat5 is violated by two records (20% of all records). Violated edits are sorted from most to least often violated. The plot visualizes the same information.

#### Error localization

The interconnectivity of edits is what makes error localization difficult. For example, the graph above shows that a record violating edit num4 may contain an error in age and/or yrsmr (years married). Suppose that we alter age so that num4 is not violated anymore. We then run the risk of violating up to *six* other edits containing age.

If we have no other information available but the edit violations, it makes sense to minimize the number of fields being altered. This principle, commonly referred to as the principle of Fellegi and Holt, is based on the idea that errors occur relatively few times and when they do, they occur randomly across variables. Over the years several algorithms have been developed to solve this minimization problem of which two have been implemented in editrules. The localizeErrors() function provides access to this functionality.

As an example we take two records from the **people** dataset from the previous subsection.

```
id <- c(2, 5)
people[id, ]
##
     age agegroup height status yearsmarried
## 2
      2
            child
                       3 married
                                            0
## 5
     34
            child
                      -7 married
                                            3
violatedEdits(E, people[id, ])
##
         edit
## record num1 num2 num3 num4 dat6 dat7 cat5 mix6 mix7
                                                                mix8
        2 FALSE FALSE FALSE FALSE FALSE FALSE TRUE TRUE FALSE FALSE
##
                TRUE FALSE FALSE FALSE FALSE TRUE FALSE FALSE
        5 FALSE
                                                               TRUE
##
        edit
##
## record mix9
        2 FALSE
##
       5 FALSE
##
```

Record 2 violates mix6 while record 5 violates edits num2, cat5, and mix8. We use localizeErrors(), with a mixed-integer programming (MIP) approach to find the minimal set of variables to adapt.

```
le <- localizeErrors(E, people[id, ], method = "mip")
le$adapt
## age agegroup height status yearsmarried
## 1 FALSE FALSE FALSE TRUE FALSE FALSE
## 2 FALSE TRUE TRUE FALSE FALSE</pre>
```

Here, the 1e object contains some processing metadata and a logical array labeled adapt which indicates the minimal set of variables to be altered in each record. It can be used in correction and imputation procedures for filling in valid values. Such procedures are not part of editrules, but for demonstration purposes we will manually fill in new values showing that the solution computed by localizeErrors() indeed allows one to repair records to full compliance with all edit rules.

```
people[2, "status"] <- "single"
people[5, "height"] <- 7
people[5, "agegroup"] <- "adult"
summary(violatedEdits(E, people[id, ]))
## No violations detected, O checks evaluated to NA
## NULL</pre>
```

The behaviour of localizeErrors() can be tuned with various options. It is possible to supply a confidence weight for each variable allowing for fine grained control on which values should be adapted. It is also possible to choose a branch-and-bound based solver (instead of the MIP solver used here), which is typically slower but allows for more control.

## 11.5.3 Correction

Correction methods aim to fix inconsistent observations by altering invalid values in a record based on information from valid values. Depending on the method this is either a single-step procedure or a two-step procedure where first, an error localization method is used to empty certain fields, followed by an imputation step.

In some cases, the cause of errors in data can be determined with enough certainty so that the solution is almost automatically known. In recent years, several such methods have been developed and implemented in the deducorrect package.

For the purposes of ADA1, we will manually correct errors, either by replacing values or by excluding observations.