

**Stat 556:**

Homework from the textbook by E.L.Lehmann

**Assignment 1 Due Sep 8 in class**

Chapter1:

P38 2.10 (for (iii) please attach your R code, Let  $\alpha=.5, 1, 2$  and  $\lambda=4, 20, 100, 500, 1000, 10000.$ )

P40 3.6 (i) (ii), 4.4

P43 5.6

**Assignment 2 Due Sep 24 in class**

Chapter2:

P119 1.7 (i)(ii)and (iii)

P121 2.10

P123 3.9

P125 4.6 and 4.7 (i), (ii) only do simulation for the  $U(-1,1)$  distribution

P127 5.5

**Assignment 3 Due October 1 in class**

Chapter2:

P130 7.11 (part (i), also assume that the sample correlation of  $(u_i, v_i)$  is bounded away from -1)

**Assignment 4 Due October 15 in class**

Chapter3:

P203 1.8 P210 3.19 (i, ii, iv) P211 4.5, 4.6

**Assignment 5 Due Nov 5 in class**

Chapter 3: P215 5.4

Chapter 4: P271 2.6, P274 3.7

Chapter 5: P359 4.9

Recommended Chap 5, 1.1, 1.2 and 1.9

**Assignment 6 Due Nov 19 in class**

Chapter 5: P360 5.7

P361 6.3, 7.3 (i)

P361 6.7 Under the hypothesis that  $p_{B|A} = p_{B|\bar{A}}$ , show that  $\text{Var}(X/m - Y/n) = Npq/mn$ ,  $p$  can be estimated by  $(X + Y)/(m + n)$ . The test obtained from (5.6.31) by replacing its denominator by  $\sqrt{\frac{N}{mn} \frac{X+Y}{m+n} (1 - \frac{X+Y}{m+n})}$  agrees with (5.6.28).

### Assignment 7 Due Dec 3 in class

Chapter 7: (1)P554 2.5 (ignore the hint for (iii))

(2) In Example 7.3.3, check that the conditions of Theorem 7.3.1 and Corollary 7.1.1 are satisfied.

(3) P559 5.1

(4) Consider the one-way random effects model with

$$Y_{ij} = \beta + v_i + \epsilon_{ij}$$

for  $i = 1, 2, \dots, n$  and  $j = 1, \dots, k$  ( $k$  is fixed), where  $v_i \sim N(0, \sigma_v^2)$ ,  $\epsilon_{ij} \sim N(0, \sigma^2)$ , and all  $v_i$  and  $\epsilon_{ij}$  are independent. Let  $\mathbf{Y}_i = (Y_{i1}, \dots, Y_{ik})'$ . Then  $\mathbf{Y}_1, \mathbf{Y}_2, \dots, \mathbf{Y}_n$  are iid  $N(\mathbf{u}, \Sigma)$ .

(a) Give  $\mathbf{u}$ ,  $\Sigma$ , and  $\Sigma^{-1}$  explicitly.

(b) Suppose the parameters of interest are  $\boldsymbol{\theta} = (\beta, \sigma^2, \sigma_v^2)'$ . What is the parameter space  $\Theta$ ?

(c) What is  $L(\boldsymbol{\theta})$ ?

(d) Find the MLE  $\hat{\boldsymbol{\theta}}$  of  $\boldsymbol{\theta}$ .

(e) Show that  $\sqrt{n}(\hat{\boldsymbol{\theta}} - \boldsymbol{\theta}) \rightarrow_L N_3(\mathbf{0}, \mathbf{V})$  and give  $\mathbf{V}$  explicitly.

(f) Now suppose we wish to estimate  $\boldsymbol{\eta} = (\beta, \sigma^2, \gamma)'$ , where  $\gamma = \sigma_v^2/\sigma^2$ . Use the delta method to find the limiting distribution of  $\sqrt{n}(\hat{\boldsymbol{\eta}} - \boldsymbol{\eta})$ .