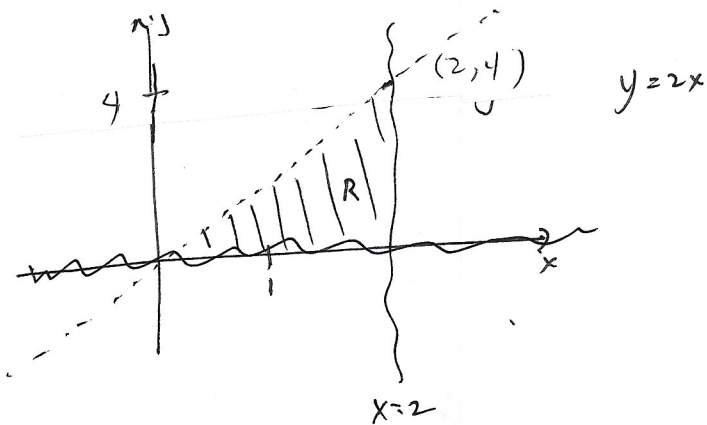


88.

$$\#_{10} f(x,y) = 2x+y$$



$$V = \iint_R f(x,y) dA$$

$$= \int_0^2 \int_0^{2x} 2x+y dy dx$$

$$= \int_0^2 \left[2xy + \frac{1}{2}y^2 \right]_0^{2x} dx$$

$$= \int_0^2 2x(2x-0) + \frac{1}{2}(4x^2) dx$$

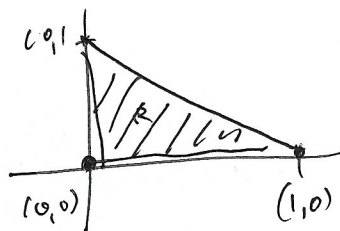
$$= \int_0^2 6x^2 dx$$

$$= 6 \cdot \frac{1}{3} x^3 \Big|_0^2$$

$$= 2(8-0)$$

$$= 16$$

#2 $f(x,y) = e^{x+2y}$



$$y = -x + 1$$

$$V = \iint_R f(x,y) dA$$

$$= \int_0^1 \int_0^{-x+1} e^{x+2y} dy dx$$

$$= \int_0^1 e^x \int_0^{-x+1} e^{2y} dy dx$$

$$= \int_0^1 e^x \left. \frac{1}{2} e^{2y} \right|_0^{-x+1} dx$$

$$= \frac{1}{2} \int_0^1 e^x (e^{2(-x+1)} - 1) dx$$

$$= \frac{1}{2} \int_0^1 e^x (e^{-2x+2} - 1) dx$$

$$= \frac{1}{2} \int_0^1 e^{-x+2} - e^x dx$$

$$= \frac{1}{2} \left(-\int_2^1 e^u du - \int_0^1 e^x dx \right)$$

$$= \frac{1}{2} \left(-e^u \Big|_2^1 - e^x \Big|_0^1 \right)$$

$$= \frac{1}{2} \left(-(e - e^2) - (e - 1) \right)$$

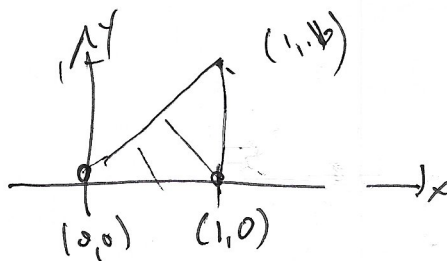
$$= \frac{1}{2} (-e + e^2 - e + 1)$$

$$= \frac{1}{2} (-2e + e^2 + 1)$$

$$= \frac{1}{2} (e - 1)^2$$

$$\begin{aligned} u &= -x+2 \\ du &= -dx \\ -du &= dx \end{aligned}$$

#18, Find Ave value
 $f(x,y) = x + 2y$



$$y = x$$

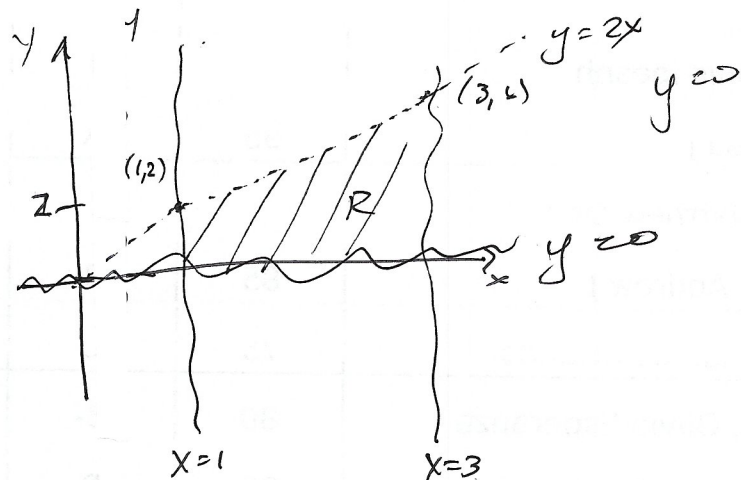
$$\text{Ave} = \frac{\iint_R f(x,y) dA}{\iint_R dA} \Rightarrow \frac{T}{B}$$

$$\begin{aligned} T &= \iint f(x,y) dA \\ &= \int_0^1 \int_0^x x + 2y \, dy dx \\ &= \int_0^1 xy + y^2 \Big|_0^x dx \\ &= \int_0^1 x(x-0) + (x^2-0) \, dx \\ &= \int_0^1 2x^2 \, dx \\ &= \frac{2}{3} x^3 \Big|_0^1 \\ &= \frac{2}{3} \end{aligned}$$

$$\begin{aligned} B &= \frac{1}{2} bh \\ &= \frac{1}{2}(1)(1) \\ &= \frac{1}{2} \end{aligned}$$

$$\begin{aligned} \text{Ave value} &= \frac{\frac{2}{3}}{\frac{1}{2}} \\ &= \frac{4}{3} \end{aligned}$$

#22. $f(x,y) = \ln x$



Ave Value

$$= \frac{\iint_R f(x,y) dA}{\iint dA} = \frac{I}{B}$$

$$\begin{aligned} \bar{f} &= \int_1^3 \int_0^{2x} \ln x \, dy \, dx \\ &= \int_1^3 \ln x \, y \Big|_0^{2x} \, dx \\ &= \int_1^3 \ln x \, (2x - 0) \, dx \\ &= \int_1^3 2x \ln x \, dx \\ &= 2 \left(\frac{1}{2} x^2 \ln x \Big|_1^3 - \frac{1}{2} \int_1^3 x \, dx \right) \\ &= 9 \ln 3 - 0 - \frac{1}{2} x^2 \Big|_1^3 \\ &= 9 \ln 3 - \frac{1}{2} (9 - 1) \\ &= 9 \ln 3 - 4 \end{aligned}$$

$$\begin{aligned} u &= \ln x & dv &= x \, dx \\ du &= \frac{1}{x} \, dx & v &= \frac{1}{2} x^2 \end{aligned}$$

B = by ^{Area} geometry Rec + Tri

$$\begin{aligned} &= 4 + \frac{1}{2} (2)(4) \\ &= 4 + 4 \\ &= 8 \end{aligned}$$

$$\begin{aligned} \text{Ave value} &= \frac{I}{B} \\ &= \frac{9 \ln 3 - 4}{8} \\ &= \end{aligned}$$

9.1

$$\# 12. y = \frac{C}{1 + Ae^{-ckt}} \quad \frac{dy}{dt} = ky(C - y)$$

$$\frac{dy}{dt} = \frac{-C(Ack e^{-ckt})}{(1 + Ae^{-ckt})^2}$$

$$= \frac{Ac^2k e^{-ckt}}{(1 + Ae^{-ckt})^2}$$

$$\frac{dy}{dt} = ky(C - y)$$

$$\frac{Ac^2k e^{-ckt}}{(1 + Ae^{-ckt})^2} = (k) \left(\frac{C}{1 + Ae^{-ckt}} \right) \left(C - \frac{C}{1 + Ae^{-ckt}} \right)$$

$$= c^2k \left(\frac{1}{1 + Ae^{-ckt}} \right) \left(1 - \frac{1}{1 + Ae^{-ckt}} \right)$$

$$= \frac{c^2k (1 + Ae^{-ckt} - 1)}{(1 + Ae^{-ckt})^2}$$

$$= \frac{c^2kAe^{-ckt}}{(1 + Ae^{-ckt})^2} \quad \checkmark$$

9.1
#18

$$y = C_1 x^3 + C_2 x^2$$

$$x^2 y'' - 4xy' + 6y = 0$$

$$y(2) = 0 \quad \& \quad y'(2) = 4$$

$$y' = 3C_1 x^2 + 2C_2 x$$

$$y'' = 6C_1 x + 2C_2$$

$$y(2) = 0$$

$$y(2) = C_1 8 + C_2 (4)$$

$$0 = 8C_1 + 4C_2$$

$$0 = 2C_1 + C_2$$

$$y'(2) = 4$$

$$y'(2) = 3C_1 4 + 2C_2 2$$

$$4 = 12C_1 + 4C_2$$

$$1 = 3C_1 + C_2$$

$$\textcircled{1} \quad 1 = 3C_1 + C_2$$

$$\textcircled{1} - \textcircled{2} \quad 3 = 2C_1 + C_2$$

$$1 = C_1 \quad \text{where} \quad C_2 = -2$$

$$\therefore y = x^3 - 2x^2$$

$$y' = 3x^2 - 4x$$

$$y'' = 6x - 4$$

check

$$x^2 y'' - 4xy' + 6y = 0$$

$$x^2(6x-4) - 4x(3x^2-4x) + 6(x^3-2x^2) = 0$$

$$\underline{6x^3 - 4x^2} - \underline{12x^3 + 16x^2} + \underline{6x^3 - 12x^2} = 0$$

$$0 = 0 \quad \checkmark$$

9.1

#24

let $S(t)$ = supply of a commodity

$$\frac{ds}{dt} = k(D(t) - s(t))$$

directly proportional
proportionality const

difference betw Demand & the supply.

#24

$$A' = C - KA$$

C = const rate g/min $\leftarrow$ (rate in)

$A(t)$ = glucose amt

$A' = \frac{dA}{dt}$ amt of change of the amt of Glucose.

KA = proportional to amt of Glucose present (rate out)

for this prob.

$$\begin{aligned} \frac{dA}{dt} &= (\text{rate in}) - (\text{rate out}) \\ &= C - KA \end{aligned}$$