

Show your work if you wish to receive credit.

1. The probability distribution of the time to complete an assembly operation is

$$f(x) = \begin{cases} 0.1 & 30 < x < 40 \text{ seconds} \\ 0 & \text{o.w.} \end{cases}.$$

- a. Determine the proportion of assemblies that requires more than 38 seconds to complete.

$$P(X > 38) = \int_{38}^{40} 0.1 dx = 0.1x \Big|_{38}^{40} = 0.2$$

- b. What time is exceeded by 90% of assemblies?

$$P(X > x) = \int_x^{40} 0.1 dx = 0.1x \Big|_x^{40} = 0.1(40 - x) = 0.9 \Leftrightarrow x = 31$$

- c. Determine the mean and variance of time of assembly.

Continuous Uniform $a=30$ $b=40$ so $E(X) = \frac{30+40}{2} = 35$ and $V(X) = \frac{(40-30)^2}{12} = \frac{100}{12} = 8\frac{1}{3}$

2. Let Z be the standard normal random variable.

a. Find $P(Z > 1.79) = .036727$

b. Find z such that $P(Z < z) = 0.75$ $z = 0.67$

3. Let X be a normal random variable with $\mu = 100$ and $\sigma = 20$.

- a. Find $P(X < 85)$

$$P(X < 85) = P\left(\frac{X-100}{20} < \frac{85-100}{20}\right) = P(Z < -0.75) = 0.226627$$

- b. Find x such that $P(X < x) = 0.75$

$$\begin{aligned} P(X < x) = 0.75 &\Leftrightarrow P\left(\frac{X-100}{20} < \frac{x-100}{20}\right) = 0.75 = P\left(Z < \frac{x-100}{20}\right) \\ &\Leftrightarrow \frac{x-100}{20} = 0.67 \Leftrightarrow x = 113.4 \end{aligned}$$