

Math. 311

Set 14

4.2, p. 196

(2, 5, 6)

4.2.2

(Is region a domain? If yes is it simply connected)

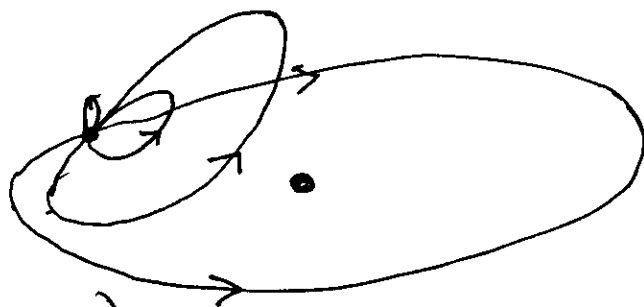
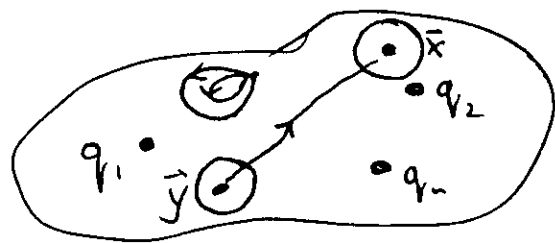
Definition: A point set that is

(i) open (each point is an interior point, i.e. $\vec{x} \in D$ means there is an open ball about \vec{x} , contained entirely in D)

(ii) connected: $\vec{x}, \vec{y} \in D \Rightarrow$ there is a curve of points in D that connect \vec{x} to \vec{y} .

(D is simply connected: any closed path ^{in D} can be shrunk down to a point without leaving D)

4.2.2 The region of definition of an electric field due to n point charges: is a simply connected domain: it is all of \mathbb{R}^3 excluding only the points where charges are situated. Then, any point is interior to D , and any loop can be shrunk to a point, avoiding the point charges



(That is possible in 3d but not in 2 dimensions!)

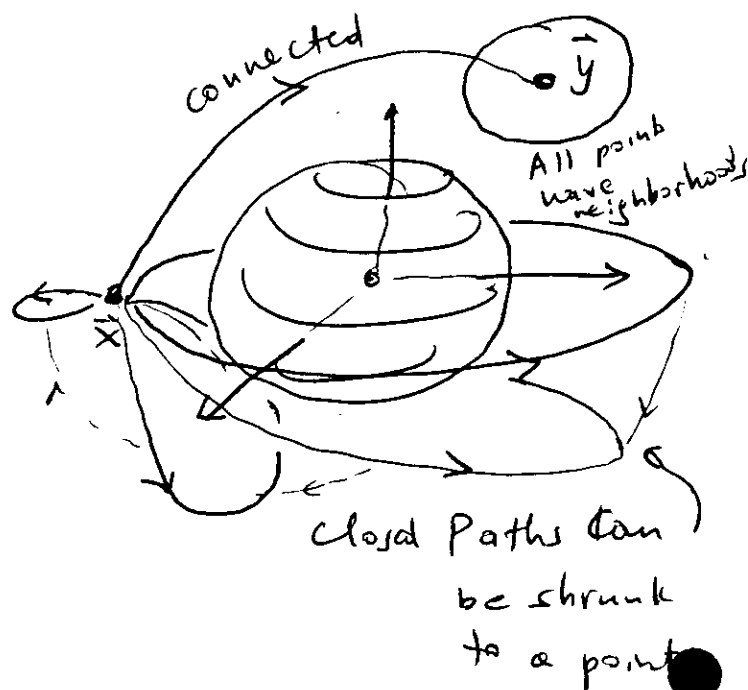
4.2.5 > The region D consisting of all points

(x, y, z) such that $x^2 + y^2 + z^2 > 4$

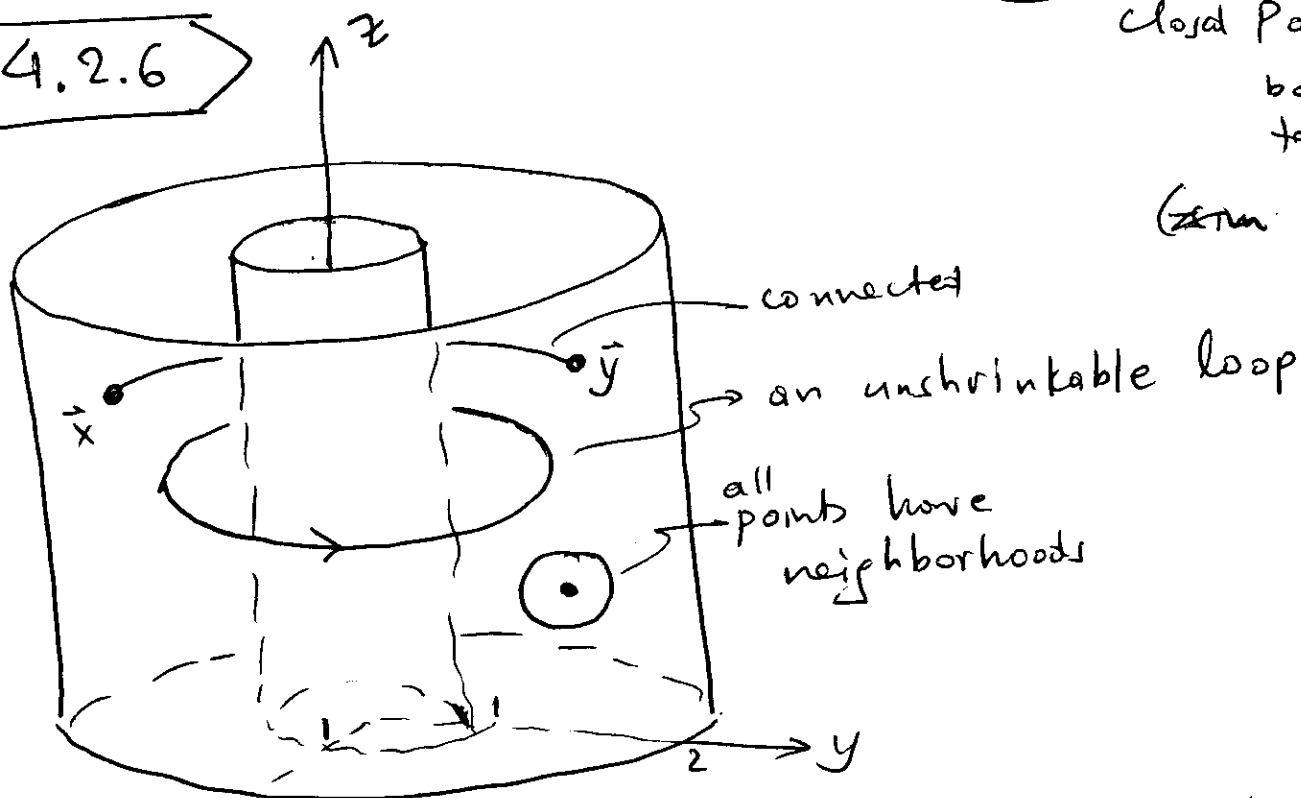
14
2/2

⚡ This is the exterior of a sphere of radius 4, center at the origin.

This is a simply connected domain



4.2.6 >



$1 < x^2 + y^2 < 4$ is the annular region between two concentric cylinders. It is open and connected, but not simply connected

⚡ It is a domain