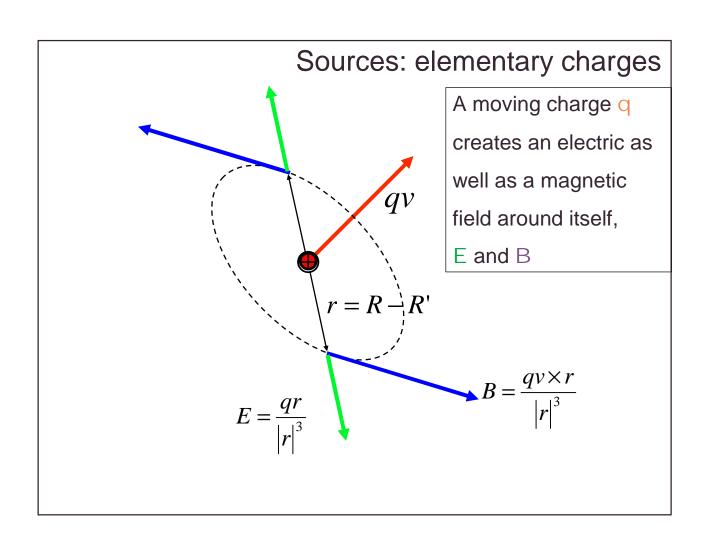
The Electric and Magnetic fields

Maxwell's equations in free space

References:

Feynman, Lectures on Physics II Davis & Snyder, Vector Analysis



A moving charge \mathbf{q} is affected by the local values of the E and B fields (Lorenz Force) $F = q(E + v \times B)$ E Cearter desiration of the E and B fields (Lorenz Force)

ME1: Sources for E field

$$\nabla \cdot E = \rho$$
 (Gauss' Law)

$$E(r) = -\frac{1}{4\pi} \iiint_{D} \frac{\rho(r')(r-r')}{|r-r'|^{3}} dV'$$

$$p(r')$$

$$r$$

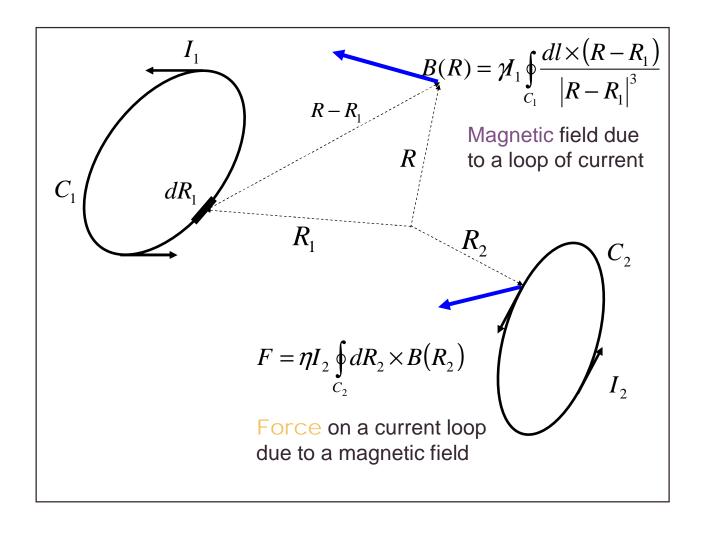
The Biot-Savart Law (magnetostatics)

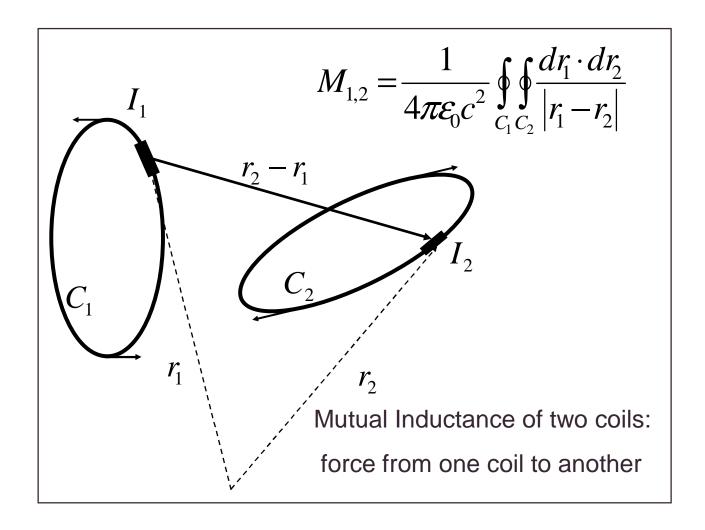
$$B(r) = \frac{1}{4\pi} \iiint_{V} \frac{J(r') \times (r-r')}{|r-r'|^{3}} dV'$$

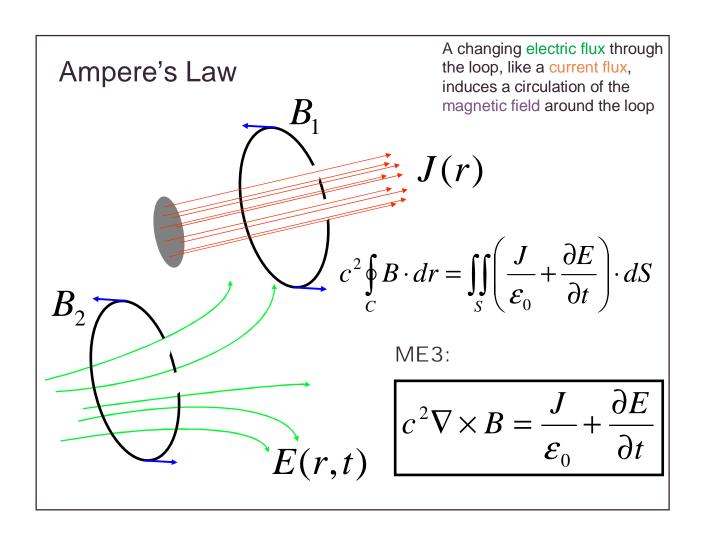
$$\nabla \cdot B = 0$$

ME2: No Magnetic Charges

$$B = \nabla \times A$$

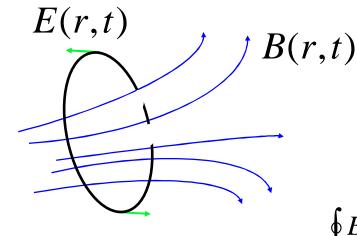








A changing magnetic flux through the loop, induces a circulation of the electric field around the loop



$$\int_{B} dx = \int_{A} \partial B dx$$

ME4:

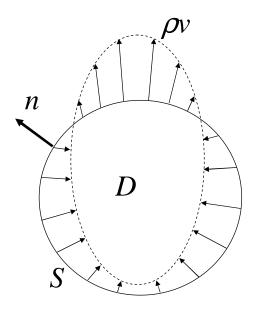
$$\nabla \times E = -\frac{\partial B}{\partial t}$$

The continuity equation

$$\frac{d}{dt} \iiint_{D} \rho(r,t) dV = - \oiint_{S} \rho v \cdot dS$$

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho v) = 0$$

The rate of change of the material (charge) in a control volume D equals the net flux into the volume



Electromagnetic waves

$$E = -\nabla \Phi - \frac{\partial A}{\partial t}$$

$$\nabla^2 \Phi - \frac{1}{c^2} \frac{\partial^2 \Phi}{\partial t^2} = -\frac{\rho}{\varepsilon_0}$$

$$\nabla^2 A - \frac{1}{c^2} \frac{\partial^2 A}{\partial t^2} = -\frac{J}{\varepsilon_0 c^2}$$

