

Solving by back-substitution:

from
back

$$\begin{pmatrix} 3 & -1 & -2 \\ 0 & 8/3 & -2/3 \\ 0 & 0 & 3/2 \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} = \begin{pmatrix} -1 \\ -4/3 \\ 2/3 \end{pmatrix}$$

$$x_3 = -\frac{14}{3}$$

$$x_2 = \frac{3}{8} \left(\frac{4}{3} + \frac{2}{3} \cdot \frac{14}{3} \right) = \frac{3}{8} \cdot \frac{40}{9} = -\frac{5}{3}$$

$$x_1 = \frac{1}{3} \left(1 + \frac{5}{3} + 2 \cdot \frac{14}{3} \right) = \frac{1}{3} \left(\frac{36}{3} \right) = 4$$

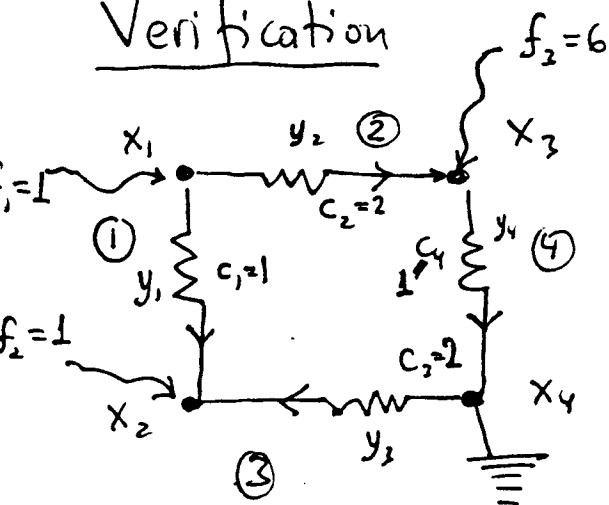
Then $y_1 = -x_1 + x_2 = -4 + \frac{5}{3} = -\frac{7}{3}$

$$y_2 = +2x_1 + 2x_3 = -8 + \frac{28}{3} = \frac{4}{3}$$

$$y_3 = -2x_2 = \frac{10}{3}$$

$$y_4 = +x_3 = -\frac{14}{3}$$

Verification



$$x_1 = -4$$

$$x_2 = -\frac{5}{3}$$

$$x_3 = -\frac{14}{3}$$

$$y_1 = -\frac{7}{3}$$

$$y_2 = \frac{4}{3}$$

$$y_3 = \frac{10}{3}$$

$$y_4 = -\frac{14}{3}$$

$$y_1 = x_2 - x_1$$

node 1: $1 + y_1 + y_2 =$

$$1 - \frac{7}{3} + \frac{4}{3} = 0$$

node 2: $1 + y_1 - y_2 =$

$$1 + \frac{7}{3} - \frac{10}{3} = 0$$

node 3: $6 + y_2 + y_4 =$

$$6 - \frac{4}{3} - \frac{14}{3} = 0$$

(node 4: $-8 + y_3 - y_4 = -8 + \frac{10}{3} - (-\frac{14}{3}) = 0$)

Kirchoff's loop law: $-4 + 4 - 4 - 4 = -\frac{8}{3} - \frac{7}{3} - \frac{5}{3} + \frac{14}{3} = 0$ compensation